# Fair Representation Learning for Recommendation: A Mutual Information Perspective (AAAI 2023) Chen et. al.

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## Introduction

2 Methodology

**B** Experiments

Image: A matrix

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- Several works exist that deal with fairness in recommendation systems
- While these models successfully mitigate unfair recommendation results to some extent, they still suffered from a substantial drop of recommendation accuracy
- Authors propose a novel two-fold MI based objective from both the user side and item side
- Authors propose the **FairMI** framework for emedding fairness in CF-based recommendations

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- U: user set (|U| = M), V: item set (|V| = N)
- $\mathbf{R} \in \mathbb{R}^{M imes N}$ : user-item interaction
- $r_{uv}$ : takes 1 when user u has interacted with item i, takes 0 if not
- $\mathcal{G} = \langle U \cup V, \mathbf{A} \rangle$ : user-item bipartite graph

### **Mutual Information**

• Shannon entropy-based measurement for the dependence between two random variable

$$\mathcal{I}(\mathbf{X};\mathbf{Y}) = \mathcal{H}(\mathbf{X}) - \mathcal{H}(\mathbf{X}|\mathbf{Y})$$
(1)

- 1 sensitive attribute encoder, 1 interest encoder, 2-fold MI based objective
- Basic idea: decompose the embedding e into a sensitive-aware embedding  $e^s$  and a sensitive-free embedding  $e^z$



Figure 1: Overall architecture

# Sensitive Attribute Encoder

$$\mathbf{h}_{v}^{k+1} = GCN\left(\mathbf{h}_{v}^{k}, \left\{\mathbf{h}_{u}^{k}: u \in \mathbf{R}_{v}\right\}\right)$$
$$\mathbf{h}_{u}^{k+1} = GCN\left(\mathbf{h}_{u}^{k}, \left\{\mathbf{h}_{v}^{k}: v \in \mathbf{R}_{u}\right\}\right)$$
(2)

- $\mathbf{R}_u$  and  $\mathbf{R}_v$  denote neighboring nodes of user u and item v
- output:  $\mathbf{e}_u^s = \mathbf{h}_u^K, \mathbf{e}_v^s = \mathbf{h}_v^K$
- Apply a sensitive attribute classifier  $S: \hat{a}_u = S(\mathbf{e}_u^s)$

$$\min_{\theta_{\mathcal{S}}, \mathbf{E}^{s}} \mathcal{L}_{A} = -\frac{1}{M} \sum_{u=1}^{M} a_{u} \log\left(\hat{a}_{u}\right)$$
(3)

#### User condition

- () Sensitive-free user embedding  $\mathbf{e}_u^z$  should have no MI with sensitive-aware user embedding  $\mathbf{e}_u^s$
- 2 Sensitive-free user embedding  $\mathbf{e}_u^z$  should have maximum MI with user interactions  $\mathbf{R}_u$ , conditioned on sesitive-aware user embedding  $\mathbf{e}_u^s$

#### Item condition

- 3 Sensitive-free item embedding  $\mathbf{e}_v^z$  should have no MI with sensitive-aware item embedding  $\mathbf{e}_v^s$
- **4** Sensitive-free item embedding  $\mathbf{e}_v^z$  should have maximum MI with user interactions  $\mathbf{R}_v$ , conditioned on sesitive-aware item embedding  $\mathbf{e}_v^s$

- Condition 1&3  $\rightarrow$  minimize  $\mathcal{I}\left(\mathbf{e}_{u}^{z};\mathbf{e}_{u}^{s}\right)$  and  $\mathcal{I}\left(\mathbf{e}_{v}^{z};\mathbf{e}_{v}^{s}\right)$
- Condition 2&4  $\rightarrow$  maximize  $\mathcal{I}(\mathbf{e}_u^z; \mathbf{R}_u | \mathbf{e}_u^s)$  and  $\mathcal{I}(\mathbf{e}_v^z; \mathbf{R}_v | \mathbf{e}_v^s)$

**Overall loss** 

$$\min_{\mathbf{E}^{z}} \mathcal{L}_{\mathsf{all}} = \mathcal{L}_{\mathsf{rec}} + \mathcal{L}_{\mathsf{MI}} \tag{4}$$

where  $\mathcal{L}_{rec}$  can be any recommendation loss (e.g. BPR loss)

# MI Upper Bound

#### Proposition 1

Given  $\mathbf{e}^s_j \sim p(\mathbf{e}^s_u)$ , if the conditional distribution  $p(\mathbf{e}^s_u | \mathbf{e}^z_u)$  is known, then

$$\mathcal{I}\left(\mathbf{e}_{u}^{s};\mathbf{e}_{u}^{z}\right) \leq \mathbb{E}\left[\log p\left(\mathbf{e}_{u}^{s}|\mathbf{e}_{u}^{z}\right) - \frac{1}{M}\sum_{j=1}^{M}\log p\left(\mathbf{e}_{j}^{s}|\mathbf{e}_{u}^{z}\right)\right]$$
(5)

$$\min_{q_{\phi}} \mathbb{D}_{\mathsf{KL}}\left[q_{\phi}(\mathbf{e}_{u}^{s}|\mathbf{e}_{u}^{z})||p(\mathbf{e}_{u}^{s}|\mathbf{e}_{u}^{z})\right] \tag{6}$$

$$\min_{\mathbf{e}_{u}^{z}} \mathcal{L}_{upper}^{user} = \frac{1}{M} \sum_{u=1}^{M} \left[ \log q_{\phi} \left( \mathbf{e}_{u}^{s} | \mathbf{e}_{u}^{z} \right) - \frac{1}{M} \sum_{j=1}^{M} \log q_{\phi} \left( \mathbf{e}_{j}^{s} | \mathbf{e}_{u}^{z} \right) \right]$$
(7)

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# MI Lower bound

Due to the high-dimension and sparsity of the user historical interactions, authors leverage a pre-trained models (e.g., BPR, LightGCN) to generate low-rank embedding  $\mathbf{p}_u$  to denote  $\mathbf{R}_u$ .

#### Proposition 2

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Given  $\mathbf{p}_u, \mathbf{e}_u^z, \mathbf{e}_u^s \sim p(\cdot, \cdot), \mathbf{p}_i \sim p(\mathbf{p}_u | \mathbf{e}_u^s)$ , with a score function f, we have

$$\mathcal{I}\left(\mathbf{e}_{u}^{z};\mathbf{p}_{u}|\mathbf{e}_{u}^{s}\right) \leq \mathbb{E}\left[\log\frac{\exp f(\mathbf{p}_{u},\mathbf{e}_{u}^{z},\mathbf{e}_{u}^{s})}{\frac{1}{M}\sum_{j=1}^{M}\exp f(\mathbf{p}_{j},\mathbf{e}_{u}^{z},\mathbf{e}_{u}^{s})}\right]$$

(8)

$$\max_{\mathbf{e}_{u}^{z}} \mathcal{L}_{\text{lower}}^{\text{user}} = \frac{1}{M} \sum_{u=1}^{M} \left[ \log \frac{\exp\left(\sin\left(\mathbf{p}_{u}, w\left(\mathbf{e}_{u}^{z}, \mathbf{e}_{u}^{s}, \alpha\right)\right)\right)}{\frac{1}{M} \sum_{j=1}^{M} \exp\left(\sin\left(\mathbf{p}_{j}, w\left(\mathbf{e}_{u}^{z}, \mathbf{e}_{u}^{s}, \alpha\right)\right)\right)} \right]$$
(9)  
where  $w\left(\mathbf{e}_{u}^{z}, \mathbf{e}_{u}^{s}, \alpha\right) = \mathbf{e}_{u}^{z} + \alpha \cdot \mathbf{e}_{u}^{s}$ . (f: weighted cosine similarity)

#### Two-fold MI based loss

$$\mathcal{L}_{\mathsf{MI}} = \beta \left( \mathcal{L}_{\mathsf{upper}}^{\mathsf{user}} + \mathcal{L}_{\mathsf{upper}}^{\mathsf{item}} \right) - \gamma \left( \mathcal{L}_{\mathsf{lower}}^{\mathsf{user}} + \mathcal{L}_{\mathsf{lower}}^{\mathsf{item}} \right)$$
(10)

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#### **3** Experiments

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- MovieLens-1M •
- Lastfm-360K
- Sensitive attribute: gender

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#### Replacement of DP

$$\forall v \in V, f_{G_0}^v = \frac{\sum_{u \in G_0} \mathbf{I}_{v \in TopK_u}}{|G_0|}, f_{G_1}^v = \frac{\sum_{u \in G_1} \mathbf{I}_{v \in TopK_u}}{|G_1|}$$
(11)  
$$\mathbf{f}_{G_0} = \left[f_{G_0}^1, \dots, f_{G_0}^v, \dots, f_{G_0}^N\right], \mathbf{f}_{G_1} = \left[f_{G_1}^1, \dots, f_{G_1}^v, \dots, f_{G_1}^N\right]$$

- $G_0, G_1$ : user group with different sensitive
- $TopK_u$ : Top-K ranked items for user u

$$DP@K = JSD(\mathbf{f}_{G_0}, \mathbf{f}_{G_1}) \tag{12}$$

# Replacement of EO similar

| К     |         | NDCG@K↑       |               | RECALL@K↑     |               | DP@K↓         |               | EO@K↓  |               |
|-------|---------|---------------|---------------|---------------|---------------|---------------|---------------|--------|---------------|
| Model |         | 10            | 20            | 10            | 20            | 10            | 20            | 10     | 20            |
| BPR   | Base    | <u>0.1943</u> | 0.2537        | 0.1437        | 0.2280        | 0.2854        | 0.2572        | 0.3580 | 0.3316        |
|       | DP      | 0.1899        | 0.2490        | 0.1409        | 0.2240        | 0.2187        | 0.1870        | 0.3231 | 0.2944        |
|       | Adv     | 0.1900        | 0.2485        | 0.1404        | 0.2230        | 0.1684        | 0.1363        | 0.2736 | 0.2499        |
|       | FairRec | 0.1896        | 0.2485        | 0.1407        | 0.2236        | 0.1656        | 0.1317        | 0.2714 | 0.2451        |
|       | FairMI* | 0.2022        | 0.2607        | <u>0.1487</u> | 0.2326        | <u>0.1501</u> | <u>0.1285</u> | 0.2406 | <u>0.2161</u> |
|       | FairMI  | 0.2022        | 0.2606        | 0.1491        | <u>0.2324</u> | 0.1381        | 0.1179        | 0.2233 | 0.2038        |
| GCN   | Base    | 0.2025        | 0.2671        | 0.1523        | 0.2449        | 0.2937        | 0.2626        | 0.3621 | 0.3325        |
|       | DP      | 0.1981        | 0.2603        | 0.1481        | 0.2363        | 0.2297        | 0.1924        | 0.3247 | 0.2955        |
|       | Adv     | 0.1970        | 0.2579        | 0.1474        | 0.2346        | 0.1517        | 0.1183        | 0.2646 | 0.2338        |
|       | FairRec | 0.1950        | 0.2561        | 0.1472        | 0.2339        | 0.1536        | 0.1193        | 0.2590 | 0.2283        |
|       | FairGo  | 0.1822        | 0.2373        | 0.1336        | 0.2108        | 0.2728        | 0.2436        | 0.3382 | 0.3101        |
|       | FairGNN | 0.1964        | 0.2569        | 0.1466        | 0.2323        | <u>0.1472</u> | <u>0.1181</u> | 0.2608 | 0.2320        |
|       | FairMI* | 0.2128        | 0.2754        | <u>0.1581</u> | <u>0.2473</u> | 0.1597        | 0.1340        | 0.2426 | 0.2243        |
|       | FairMI  | 0.2128        | <u>0.2752</u> | 0.1586        | 0.2477        | 0.1337        | 0.1111        | 0.2228 | 0.2006        |

Figure 2: MovieLens-1M

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- (Ablation study) Effectiveness of Lower bound and Upper bound
- (Parameter sensitivity analysis) different  $\beta$  and  $\gamma$

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